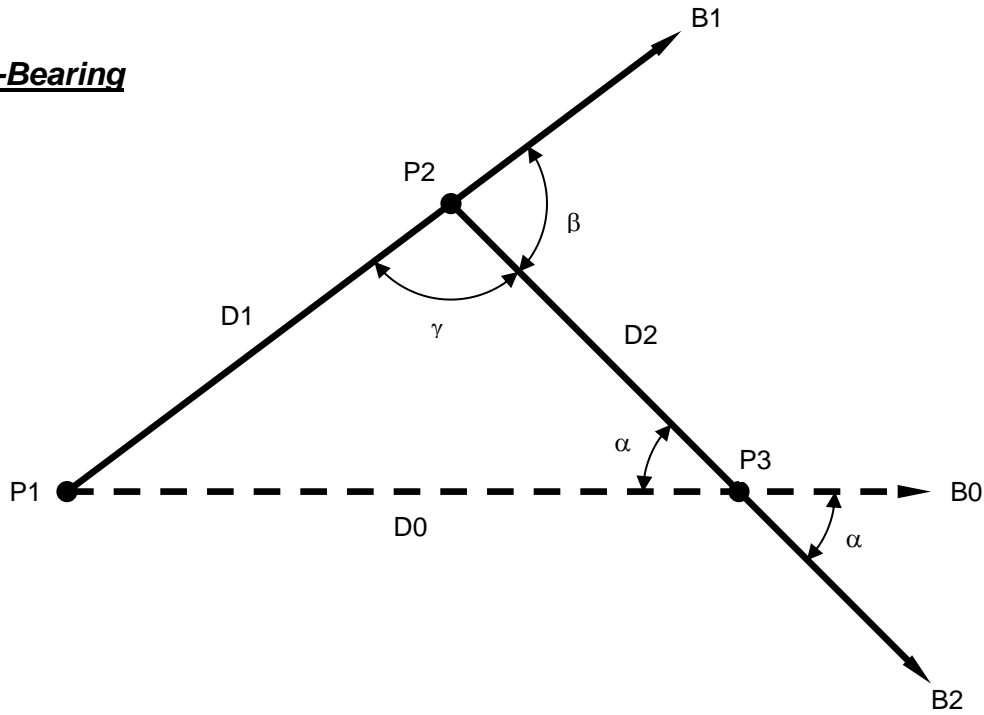


**Bearing-Bearing**



Note:	P1, P3 known implies...	B0, D0 known
Given:	B0	base bearing (azimuth)
	D0	base distance
	B1	initial bearing (azimuth)
	B2	closing bearing (azimuth)
Find:	D1	initial distance...

$$\alpha = B2 - B0$$

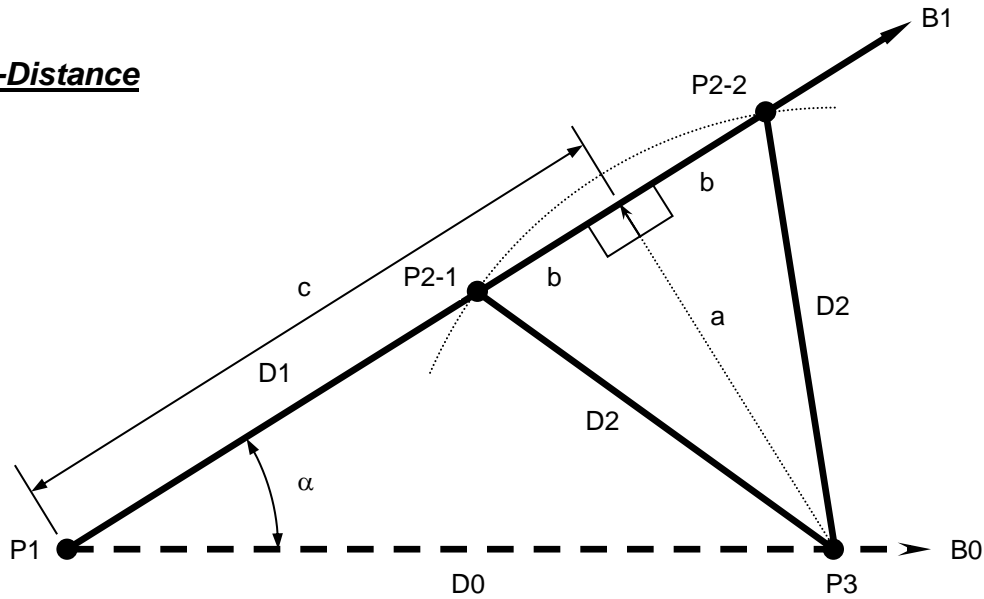
$$\beta = B2 - B1$$

$$\sin(\gamma) = \sin(\beta)$$

$$\frac{D1}{\sin(\alpha)} = \frac{D0}{\sin(\gamma)}$$

$$B1 = D0 \cdot \frac{\sin(B2 - B0)}{\sin(B2 - B1)}$$

**Bearing-Distance**



Note: P1, P3 known implies... B0, D0 known

Given: B0 base bearing (azimuth)  
 D0 base distance  
 B1 initial bearing (azimuth)  
 D2 closing distance

Find: D1 initial distance...

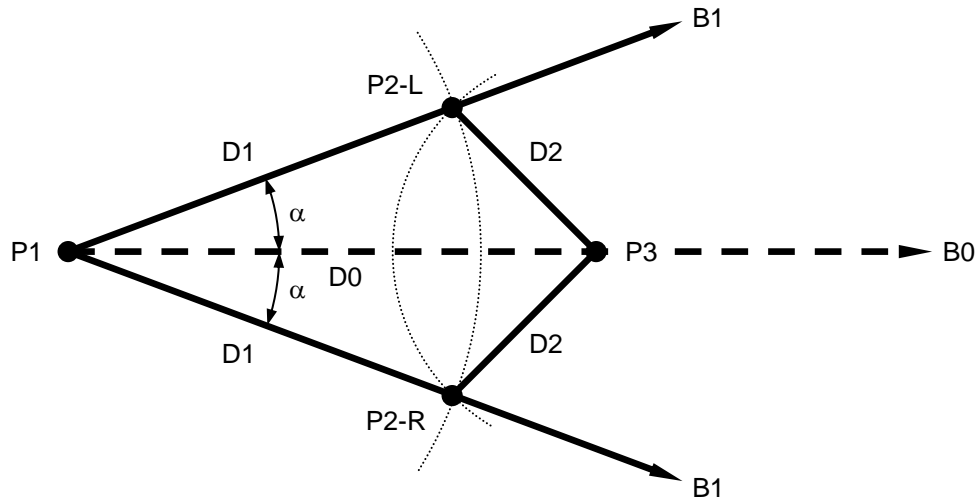
$$\alpha = B0 - B1$$

$$a = D0 \cdot \sin(\alpha) \quad c = D0 \cdot \cos(\alpha)$$

$$b^2 = D2^2 - a^2$$

$$D1 = c \pm b$$

$$D1 = D0 \cdot \cos(B0 - B1) \pm \sqrt{D2^2 - D0^2 \cdot \sin^2(B0 - B1)}$$

**Distance-Distance**

Note:	P1, P3 known implies...	B0, D0 known
Given:	B0 base bearing D0 base distance D1 initial distance D2 closing distance	(azimuth)
Find:	B1 initial bearing...	

$$D2^2 = D0^2 + D1^2 - 2 \cdot D0 \cdot D1 \cdot \cos(\alpha)$$

$$\alpha = \text{acos} \left( \frac{D0^2 + D1^2 - D2^2}{2 \cdot D0 \cdot D1} \right)$$

$$B1 = B0 \pm \alpha$$

$$B1 = B0 \pm \text{acos} \left( \frac{D0^2 + D1^2 - D2^2}{2 \cdot D0 \cdot D1} \right)$$