

$$G1 \cdot \frac{L}{2} + G2 \cdot \frac{L}{2} = G1 \cdot L + TO$$

$$TO = G2 \cdot \frac{L}{2} + G1 \cdot \frac{L}{2} - G1 \cdot L$$

$$TO = G2 \cdot \frac{L}{2} - G1 \cdot \frac{L}{2}$$

$$TO = \frac{L}{2} \cdot (G2 - G1)$$

Linear:  $y = B \cdot x + C$

Quadratic:  $y = A \cdot x^2 + B \cdot x + C$

New Elev = Grade x Dist + Elev

New Elev = TO + Grade x Dist + PVC Elev

$$A \cdot x^2 = \frac{L}{2} \cdot (G2 - G1)$$

$$A = \frac{L}{2 \cdot x^2} \cdot (G2 - G1)$$

Since  $x = L \dots$

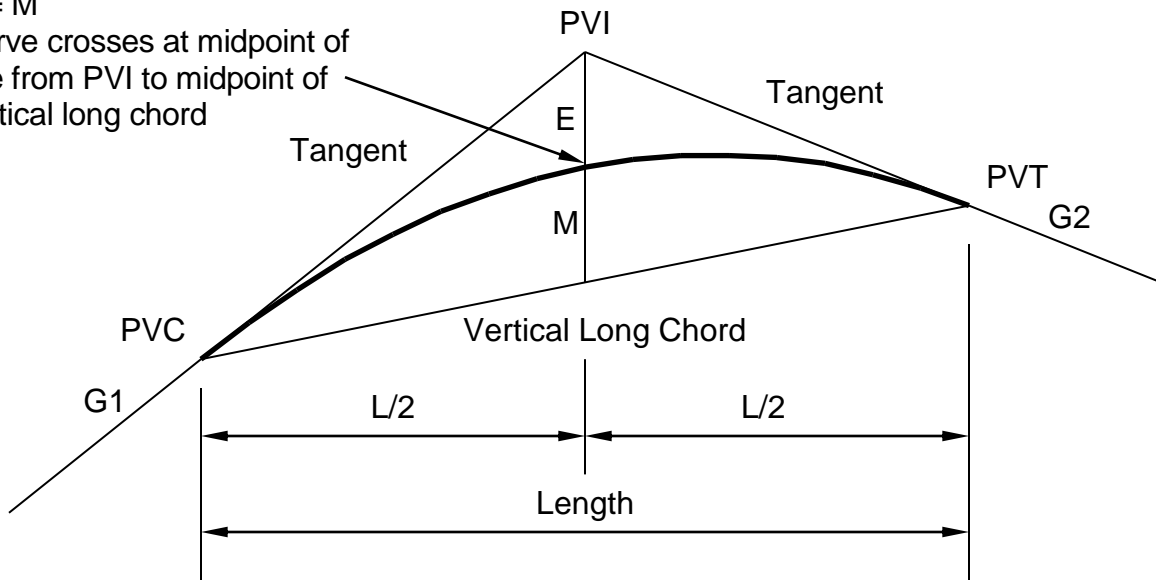
$$A = \frac{(G2 - G1)}{2 \cdot L}$$

Note:  $r = \frac{(G2 - G1)}{L} = 2 \cdot A$

$$B = G1$$

$E = M$

Curve crosses at midpoint of line from PVI to midpoint of vertical long chord



- PVC = Point of Vertical Curvature
- PVI = Point of Vertical Intersection
- PVT = Point of Vertical Tangency
- E = External Secant
- M = Middle Ordinate
- G1 = Grade 1, Entering Gradient
- G2 = Grade 2, Exiting Gradient

To solve for the tangent offset distance at any station (STA) along the tangent:

Entering Curve: 
$$\text{Tangent Offset} = E \cdot \left( \frac{\text{STA} - \text{PVCsta}}{\text{PVIsta} - \text{PVCsta}} \right)^2$$

Exiting Curve: 
$$\text{Tangent Offset} = E \cdot \left( \frac{\text{PVTsta} - \text{STA}}{\text{PVTsta} - \text{PVIsta}} \right)^2$$

PROPERTIES  
of  
SYMMETRICAL or EQUAL TANGENT  
VERTICAL CURVES

1. "M" = "E"  
That is to say that the curve lies midway (vertically) between the elevation of the PVI and the elevation of the midpoint of the "chord".
2. Offsets from the two straight grade lines are symmetrical on either side of the PVI. Equal distances yield equal tangent offsets.
3. Tangent offsets from either grade line vary with the square of the distance from the point of tangency of that grade line.